The impact of pore size distribution data presentation format on pore structure interpretation of shales

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Abstract: A deeper understanding of pore structures in unconventional shale plays can lead to a better evaluation of storage and transport capacity in these complicated rock types. This task is usually done through pore size distribution (PSD) analysis. In this study, \( \text{N}_2 \) adsorption and high-pressure mercury intrusion porosimetry (MIP) were employed to investigate several shale samples. Three different mathematical forms of PSD data presentation: Incremental pore volume versus diameter (\( DV \)), differential pore volume versus diameter (\( DV/Dd \)) and the log differential pore volume versus diameter (\( DV/D \log d \)), were used to analyze pore structures from these two different methods. The comparison of the results showed that each form of PSD data presentation could demonstrate various types of important pore information. The \( DV \) curve is significantly dependent on the experimental data points’ spacing while the other two are not affected. The \( DV/Dd \) curve would incite the existence of smaller pore ranges while the \( DV/D \log d \) would embolden larger pore ranges. Additionally, multifractal analysis from each data presentation style illustrated that the heterogeneity index of PSD calculated from the \( DV/Dd \) curve is much significant than the one obtained from the \( DV/D \log d \) curve. \( DV/Dd \) is more appropriate to be used for characterizing PSD data from \( \text{N}_2 \) adsorption while \( DV/D \log d \) is preferred when MIP data is collected from larger pores.

1. Introduction

As a typical unconventional reservoir, nowadays shales contribute to a large portion of the total oil/gas production in the world. The pore spaces in the shale rocks are the place where hydrocarbons are accumulated, while the size of these pores could affect the transporting behavior of the rock medium (Liu and Peyman, 2017). Thus, accurately characterizing the pore size distribution of the shale rocks is essential. During the past decade, many researchers have investigated the pore structures of different shale plays in the world (Yang et al., 2015; Wang et al., 2016, 2019; Kumar et al., 2019). In this regard, fluid invasion methods such as the gas adsorption and high-pressure mercury intrusion porosimetry (MIP) are widely applied in characterizing the pore structures of shale rocks (Bustin et al., 2008; Clarkson et al., 2012, 2013; Gao and Hu, 2013; Mastalerz et al., 2013; Tang et al., 2015; Han et al., 2016; Liu et al., 2017, 2019a; Zou et al., 2017; Yuan et al., 2018). It is known that in nitrogen adsorption, as the relative pressure (the ratio of the gas vapor pressure in the system and the saturation pressure of nitrogen) increases, the adsorption quantity will increase (Thommes et al., 2015). This will enable the estimation of pore volume based on the assumption of the existence of certain pore shapes within the sample. In high-pressure mercury intrusion, Washburn equation is commonly employed to quantify the pore sizes (Washburn, 1921). The pore size distribution derived from these two latest methods is usually expressed in the form of a pore volume distribution as a function of the pore diameter/radius. Incremental pore volume versus diameter (\( DV \)), differential pore volume versus diameter (\( DV/Dd \)) and the log differential pore volume versus diameter (\( DV/D \log d \)) are three main presentations that researchers use to display pore size distributions. These three presentations of the pore size can be calculated through the following equations (Meyer and Klobes, 1999):

\[
DV = V_{i+1} - V_i \quad (1)
\]

\[
DV/Dd = \frac{V_{i+1} - V_i}{d_{i+1} - d_i} \quad (2)
\]

\[
DV/D \log d = \frac{V_{i+1} - V_i}{\log d_{i+1} - \log d_i} \quad (3)
\]
where $V_i$ is the cumulative pore volume at the pressure point ($P_i$) and $V_{i+1}$ is the cumulative pore volume at a higher-pressure ($P_{i+1}$). $d_{i+1}$ refers to the pore diameter where the cumulative pore volume is $V_{i+1}$ and $d_i$ donates the pore diameter where the cumulative pore volume is $V_i$.

Choosing the most appropriate form of presentation of pore size distribution (PSD) could affect the pore structure interpretations. This discrepancy in interpretation of the results, originates from different mathematical concepts that these methods rely on. However, to the authors’ knowledge, very few studies are available that compares these different presentations and the outcomes, specifically related to the pore structure characterization of shales. In certain methods, such as $N_2$ adsorption, some researchers utilized the $DV$ (Cao et al., 2015) while other researchers employed $DV/Dd$ (Kuila, 2013) or $DV/D\log d$ (Clarkson et al., 2013; Liu et al., 2017). However, the question remains how each presentations method would interpret the data and the superiority of one over the other to better characterize the pore structures of the shale with $N_2$ adsorption or mercury intrusion, in particular.

In this paper, we analyzed pore structure data and compared different forms of presentations of the PSD data from shale rocks that were acquired by $N_2$ adsorption and high-pressure mercury intrusion methods. The main goal of this paper is to add more knowledge to our understanding from the pore structure of shale rocks through in-depth data analysis and comparison by answering the following questions: 1) What is the difference between these different common forms of data presentations? Also, 2) which presentation is preferred for the $N_2$ adsorption and which one is more suited towards high-pressure mercury intrusion.

### 2. Case study and discussions

#### 2.1 $N_2$ adsorption

6 shale samples were crushed into powders and then degassed for more than 8 hours at 110 °C (Liu et al., 2019b). It is well known that grain sizes could affect data analysis and the results (Hazra et al., 2018), thus, in order to limit grain size effect, in this study, samples were prepared to have grain sizes less than 250 $\mu$m. Then $N_2$ adsorption experiment was performed with the Micromeritics® Tristar II apparatus at 77 K. The gas adsorption volume was measured over the relative equilibrium adsorption pressure ($P/P_0$) ranging from 0.01 to 0.99. After that, the pore size distributions of the samples were calculated using the density functional theory (Do and Do, 2003).

The major mineral compositions and the total organic carbon (TOC) content of the samples that were tested by $N_2$ adsorption can be seen in Table 1. The results showed samples having different mineral compositions and TOC content. Quartz and clay are the major minerals in Sample #1 to Sample #4 while the dominant mineral in Sample #5 and Sample #6 were carbonate minerals. Sample #2 has the largest TOC content (17.7 wt. %) while Sample #6 has the smallest TOC content (4.8 wt. %).

The simplest way to display pore size distribution is to plot the incremental pore volume versus the pore diameter. Fig. 1 shows the incremental pore volume curves of two representative samples (Sample #1 and Sample #2). Both curves exhibit the multimodal peaks, depicting the complexity of the pore structures. The largest peak exists between the pore size intervals from 20 nm to 30 nm for both samples, indicating that the pores with sizes from 20-30 nm contribute the most to the porosity of the samples when the PSD data is presented in this specific style. $DV$ curve is the true pore volume distribution that is a function of pore diameter. However, the peak values from this distribution are dependent on the experiment spacing data points since more pore volume will be accumulated by summation in a larger pore radius interval than in the smaller ones (Meyer and Klobes, 1999). The limit of the pore size that can be measured by $N_2$ adsorption is less than 200 nm. In this experiment, relative pressure was increased from 0 to 0.99 linearly, while, based on Kelvin’s equation, the relationship between the pore diameter and the relative pressure is non-linear. The incremental pore diameter between the two neighboring experimental data point is increasing as the pore size increases. In order to avoid the effect that spacing between data points would have on the pore size distribution, two other presentations of pore size distribution: Differential pore volume distribution and log differential pore volume distribution are developed.

![Image](image_url)

Table 1. Mineral compositions of the samples tested for the $N_2$ gas adsorption.

<table>
<thead>
<tr>
<th>Samples</th>
<th>Quartz (wt. %)</th>
<th>Feldspar (wt. %)</th>
<th>Carbonate (wt. %)</th>
<th>Pyrite (wt. %)</th>
<th>Clay (wt. %)</th>
<th>TOC (wt. %)</th>
</tr>
</thead>
<tbody>
<tr>
<td>#1</td>
<td>60.2</td>
<td>8.1</td>
<td>–</td>
<td>2.4</td>
<td>20.8</td>
<td>13.1</td>
</tr>
<tr>
<td>#2</td>
<td>46.1</td>
<td>1.3</td>
<td>–</td>
<td>15</td>
<td>32.3</td>
<td>17.7</td>
</tr>
<tr>
<td>#3</td>
<td>57.8</td>
<td>10.7</td>
<td>2.1</td>
<td>3.9</td>
<td>20.3</td>
<td>5.4</td>
</tr>
<tr>
<td>#4</td>
<td>55.1</td>
<td>1.2</td>
<td>2.1</td>
<td>15</td>
<td>32.3</td>
<td>17.7</td>
</tr>
<tr>
<td>#5</td>
<td>15.1</td>
<td>2.1</td>
<td>22.1</td>
<td>2.2</td>
<td>2.4</td>
<td>5.9</td>
</tr>
<tr>
<td>#6</td>
<td>30.6</td>
<td>2.0</td>
<td>46.6</td>
<td>1.7</td>
<td>14.9</td>
<td>4.8</td>
</tr>
</tbody>
</table>

![Image](image_url)
Fig. 1. Examples of the incremental pore volume versus the pore diameter.

Fig. 2. Comparison of the $DV$ curve (black) and the $DV/Dd$ curve (blue).

Fig. 3. Comparison of the $DV/Dd$ curve (blue) and the $DV/D\log d$ curve (red).
Fig. 2, the major peak representing dominant pore sizes is found around 20 to 30 nm by the $DV$ curve, while the major peak of the $DV/Dd$ curve (blue) is observed around 2-4 nm as the dominant pore size.

The log differential pore volume distribution curve ($DV/D \log d$) and the differential pore volume distribution curve ($DV/Dd$) of Sample #1 and Sample #2 can be seen in Fig. 3. The largest peak of the $DV/D \log d$ curve is around 20-30nm which is closer to the location of the largest peak in the $DV$ curve (Fig. 3). The location of the peaks can be derived from the deconvolution method. The details of this procedure can be seen in the appendix. The deconvolution of the $DV/Dd$ curve and the $DV/D \log d$ curve of Sample #1 and Sample #2 can be found in Fig. 4 and Fig. 5, respectively. Considering Sample #1 for instance, both $DV/Dd$ and $DV/D \log d$ curves can be deconvoluted into 5 different phases. The deconvolution summary results from all of the samples based on $N_2$ adsorption data can be seen in Table 2. Considering Sample #1 for instance, the peaks of the pore size range of 10-40 nm can be seen in both $DV/Dd$ and the $DV/D \log d$ curves, meaning that these peaks are not affected with the style of PSD data presentations. On the contrary, considering Sample #3, comparing $DV/D \log d$ and $DV/Dd$ curves, the latest, shows the presence of additional peaks in the smaller pore radius range while $DV/D \log d$ provides us with peaks in the larger pore size ranges. Based on the results from this step, it can be said that $DV/Dd$ curve can reflect more information about the pores in the smaller radius range while $DV/D \log d$ in the larger pore radius range.

Pore size distribution data can be used to quantify the heterogeneity of pore structures. In this section, multifractal analysis is employed to analyze and compare the heterogeneity index of pore size distributions from these two different presentations ($DV/Dd$ and $DV/D \log d$). The detail of multi-
Table 2. The deconvolution results of two different presentations from N\textsubscript{2} adsorption.

<table>
<thead>
<tr>
<th>Samples</th>
<th>Phase 1</th>
<th>Phase 2</th>
<th>Phase 3</th>
<th>Phase 4</th>
<th>Phase 5</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Mean (nm)</td>
<td>Sd (nm)</td>
<td>Mean (nm)</td>
<td>Sd (nm)</td>
<td>Mean (nm)</td>
</tr>
<tr>
<td>#1</td>
<td>2.78</td>
<td>0.06</td>
<td>4.36</td>
<td>0.68</td>
<td>7.89</td>
</tr>
<tr>
<td>2</td>
<td>3.11</td>
<td>0.13</td>
<td>5.06</td>
<td>0.43</td>
<td>9.92</td>
</tr>
<tr>
<td>#2</td>
<td>2.89</td>
<td>0.03</td>
<td>4.63</td>
<td>0.18</td>
<td>9.33</td>
</tr>
<tr>
<td>2</td>
<td>2.96</td>
<td>0.16</td>
<td>5.18</td>
<td>0.68</td>
<td>10.23</td>
</tr>
<tr>
<td>#3</td>
<td>2.73</td>
<td>0.04</td>
<td>3.82</td>
<td>0.39</td>
<td>6.04</td>
</tr>
<tr>
<td>2</td>
<td>2.97</td>
<td>0.04</td>
<td>5.83</td>
<td>0.22</td>
<td>10.72</td>
</tr>
<tr>
<td>#4</td>
<td>8.27</td>
<td>0.64</td>
<td>12.42</td>
<td>1.71</td>
<td>19.87</td>
</tr>
<tr>
<td>2</td>
<td>9.50</td>
<td>1.87</td>
<td>15.82</td>
<td>4.76</td>
<td>22.07</td>
</tr>
<tr>
<td>#5</td>
<td>3.21</td>
<td>0.03</td>
<td>4.73</td>
<td>0.18</td>
<td>9.97</td>
</tr>
<tr>
<td>2</td>
<td>3.28</td>
<td>0.29</td>
<td>8.85</td>
<td>2.04</td>
<td>12.75</td>
</tr>
<tr>
<td>#6</td>
<td>3.04</td>
<td>0.05</td>
<td>4.27</td>
<td>0.31</td>
<td>8.48</td>
</tr>
<tr>
<td>2</td>
<td>3.13</td>
<td>0.14</td>
<td>4.65</td>
<td>0.63</td>
<td>9.57</td>
</tr>
</tbody>
</table>

Note: Sd means the standard deviation, 1 refers to the DV/D\textsubscript{d} curve while 2 denotes the DV/D\textsubscript{log d} curve.

Table 3. Summary of multifractal analysis from these two different presentations obtained from N\textsubscript{2} adsorption.

<table>
<thead>
<tr>
<th>Samples</th>
<th>DV/D\textsubscript{d}</th>
<th>DV/D\textsubscript{log d}</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>(\alpha_{-10})</td>
<td>(\alpha_0)</td>
</tr>
<tr>
<td>#1</td>
<td>2.4862</td>
<td>1.6404</td>
</tr>
<tr>
<td>#2</td>
<td>2.1494</td>
<td>1.4358</td>
</tr>
<tr>
<td>#3</td>
<td>2.2335</td>
<td>1.5762</td>
</tr>
<tr>
<td>#4</td>
<td>1.7134</td>
<td>1.2440</td>
</tr>
<tr>
<td>#5</td>
<td>1.7221</td>
<td>1.3150</td>
</tr>
<tr>
<td>#6</td>
<td>2.1284</td>
<td>1.5317</td>
</tr>
</tbody>
</table>

Fig. 6. The relationship between \(\alpha_q\) and \(q\) in Sample #4.
Table 4. Mineral compositions of the samples for the mercury intrusion test.

<table>
<thead>
<tr>
<th>Samples</th>
<th>Quartz (wt. %)</th>
<th>Pyrite (wt. %)</th>
<th>Feldspar (wt. %)</th>
<th>Dolomite (wt. %)</th>
<th>Clay (wt. %)</th>
<th>TOC (wt. %)</th>
</tr>
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<tbody>
<tr>
<td>#7</td>
<td>70.3</td>
<td>3.2</td>
<td>7.7</td>
<td>0.0</td>
<td>18.8</td>
<td>14.2</td>
</tr>
<tr>
<td>#8</td>
<td>54.3</td>
<td>8.1</td>
<td>0.0</td>
<td>8.8</td>
<td>28.6</td>
<td>20.2</td>
</tr>
<tr>
<td>#9</td>
<td>66.9</td>
<td>2.4</td>
<td>14.4</td>
<td>0.0</td>
<td>16.2</td>
<td>11.1</td>
</tr>
<tr>
<td>#10</td>
<td>70.0</td>
<td>2.4</td>
<td>5.5</td>
<td>0.0</td>
<td>22.2</td>
<td>12.2</td>
</tr>
<tr>
<td>#11</td>
<td>36.1</td>
<td>8.5</td>
<td>3.4</td>
<td>0.0</td>
<td>52.0</td>
<td>14.9</td>
</tr>
</tbody>
</table>

Fig. 7. Relationship between heterogeneity index of the pore size distributions obtained from two different presentations in the samples (Sample #1 - Sample #6).

parameters that are calculated from the $DV/D\log d$ curve. However, $DV/D\log d$ curve has a larger $\alpha_{10}$ value. The heterogeneity index that is calculated from the $DV/Dd$ curve is greater than the heterogeneity index from the $DV/D\log d$ curve. Fig. 7 compares the heterogeneity index estimated from these two different presentations where a linear correlation can be found between them. Collectively, the multifractal analysis results showed that heterogeneity of the pore size distributions calculated from the $DV/Dd$ curve is more significant compared to the $DV/D\log d$ in the same sample.

The impact of rock compositions (mineral and organic part) on the heterogeneity index is further analyzed and discussed here. The partial linear least square regression method was employed which is found to be a suitable form of analysis that would exist between PSD heterogeneity and rock composition (Liu et al., 2017). The rock compositions including the minerals and the organic matter will be considered as the independent parameters while the heterogeneity index can be viewed as the dependent parameters. The results in Fig. 8 show that feldspar has the most significant effect on the heterogeneity index of both presentations. Carbonate has a negative effect on the heterogeneity index while the other constituent components would have a positive effect on PSD heterogeneity. To summarize, the effect of rock compositions on the heterogeneity index that is obtained from these two presentations is similar while the intensity is quite different. $DV/Dd$ curve for example, the effect that rock compositions have on the heterogeneity index based on their order of the intensity is: Feldspar > clay > organic matter, while in the $DV/D\log d$ curve, this order follows: Feldspar > organic matter > clay.

2.2 High pressure mercury intrusion

Another important method to characterize pore structures of shale or any rock medium is high pressure mercury intrusion porosimetry. In this part, additional five samples (Sample #7, #8, #9, #10, #11) were collected and analyzed with MIP (Liu et al., 2019a). After being vacuum-dried in the oven at 70 °C for over 10 hours, the samples were put in the mercury porosimeter (Auto Pore IV 9510, Micrometrics Instrument). Capillary pressure curves vs. the volume of mercury intruding sample pores were recorded as the injection pressure is increased from 0 psi up to 60000 psia (413.68 MPa) (Liu et al., 2019a). The mineral compositions of these five samples are presented in Table 4, indicating that quartz and clay are the major components of these rock samples. All the samples are organic rich with TOC content more than 10 wt. %.

The black curve in Fig. 9 represents the $DV$ curve and the blue curve denotes the $DV/Dd$ curve data presentation. Both curves have noticeable unimodal characteristics. Alike the $N_2$ adsorption data, where the major peak appears is different in each form of PSD data presentation. In this regard, the major peak of the $DV$ curve is found in larger pore radii in comparison to the major peak of the $DV/Dd$. 
A better comparison of $DV/Dd$ curve and the $DV/D\log d$ curve can be seen in Fig. 10 where major differences can be distinguished between the two curves. The blue curve ($DV/Dd$) shows the unimodal characteristics while the red curve ($DV/D\log d$) from the same sample has a multimodal behavior where several peaks (pore diameters) exist in the $DV/D\log d$ curve that are missing in the $DV/Dd$ curve. Taking Sample #7 for example, the peak that is associated with the pore size diameter of around 500 nm exists in the $DV/D\log d$ curve but cannot be distinguished in the $DV/Dd$ curve. Additionally, major peaks of the $DV/D\log d$ curve correspond to larger pore sizes than major peaks in $DV/Dd$ curve.

Following the same analysis that was carried out for the $N_2$ adsorption, the heterogeneity parameters of these two different presentations ($DV/Dd$ and $DV/D\log d$) were compared. The correlations between $\alpha_q$ and $q$ of Sample #7 and Sample #8 is displayed in Fig. 11. Considering both curves in the same sample, $\alpha_0 > \alpha_1 > \alpha_2$ explains that mercury intrusion has the multifractal characteristics in both form of presentation of the data. The comparison of the heterogeneity indices of the pore size distributions from these two different presentations is depicted in Fig. 12. The results show that heterogeneity index values that are obtained from the $DV/Dd$ curve are generally larger than values that are obtained from the $DV/D\log d$ curve.

The impact that rock composition would have on the heterogeneity index from these two different presentations can be seen in Fig. 13. The results indicate that the impact of rock compositions on the heterogeneity index of these two different presentations are similar based on individual component. For example, organic matter has the most significant positive effect on the heterogeneity index while clay has a negative impact on the heterogeneity index that is calculated from these two different presentations. Furthermore, the magnitude of this impact from individual components on heterogeneity index of these two different presentations follows the same order.

3. Recommendations

The analysis that was laid out above demonstrate that diff-
different form of presentations of PSD data can lead to a different interpretation of the data such as the location of major peaks (pore size), peak intensity (pore frequency), the resulting heterogeneity and the impact of rock compositions on the heterogeneity index. Furthermore, the differential pore volume distribution is defined as the difference between two diameter boundaries over which the volume is determined. Considering this definition, the endpoints in the PSD intervals and the magnitude of their expression plays a major role in the results. The upper endpoint may be expressed in tens of nanometers ($N_2$ gas adsorption) or hundreds of micrometers (mercury intrusion) while the lower endpoint will be around less than 1 nanometer ($N_2$ adsorption) or few nanometers (mercury intrusion), respectively. Particularly in MIP for example, the endpoints that are either expressed in micrometer or nanometer ([50 µm-100 µm] or [5 nm-10 nm], for example), the increments will represent equal distances along the x-axis if they are plotted in the logarithmic scale. Considering the intrusion volume (1 mL/g) over these two amount of interval increments (50 µm, 5 nm, respectively), the differential pore volume per diameter over these increments will be 0.02 and 200 mL/g/µm, respectively. For the equal amount of pore volumes, the intensity of the $DV/Dd$ at one interval (100 µm-50 µm) is only around 0.01% of the other interval (10 nm-5 nm). This means, the presentation of the $DV/Dd$ curve can signify the role that smaller pore diameter ranges would have on PSD data while suppressing the contribution from larger pore diameter intervals.

From mathematics point of view, the correlation between $DV/D \log d$ and $DV/Dd$ is defined by the following equation (Meyer and Klobes, 1999):

$$\frac{DV}{D \log r} = 2.303r \frac{DV}{Dr}$$

where $r$ is the radius of the pore.

Fig. 11. The correlations between the $α_q$ and $q$.

Fig. 12. Relationship between heterogeneity index of pore size distribution data from two different presentations (Sample #7 to Sample #11).

Fig. 13. The influence of individual minerals/TOC on the heterogeneity from the pore size distribution data from the two different presentations.
where $r$ is the pore radius.

It’s found in Eq. (4), that the $2.303r$ term is the weighting parameter for the $DV/D\log d$ curve which will magnify the impact of pores at larger radii. MIP intervals that were used above, for example, the log difference between the largest incremental interval ($\log (100\ \mu m)$-$\log (50\ \mu m)$) will be 0.3 which is close to the log difference of the smallest incremental interval ($\log(0.01\ \mu m)$-$\log(0.005\ \mu m)$) of pore diameters. If the intrusion volume (1 mL/g) over these two interval increments was the same, then the intensity of the peaks for $\log$ differential pore volume distributions at both ends will be similar.

Overall, the $DV/Dd$ will magnify the smaller pore ranges and suppress the larger pore ranges while the $DV/D\log d$ has an opposite effect. In shale samples, the $N_2$ adsorption can measure the smaller pores ranges from 2-200 nm with the majority of the pores from 2-50 nm thus the $DV/Dd$ curve is preferred which can better characterize PSD. On the contrary, in mercury intrusion, since the high pressure from the mercury intruding the pores can distort pore structures, especially in smaller ones due to the compressibility effects, one can conclude the smaller pore diameter ranges that are obtained from the mercury intrusion might not be accurate. Therefore, in order to suppress the effect from the contributing or occupied smaller pores, the $DV/D\log d$ curve is preferred for data presentation in MIP. In this study, the goal was to focus on the effect of the presentations on the PSD interpretations from two mainstream experimental methods, the $N_2$ gas adsorption and MIP, which can characterize the pores with sizes larger than 2 nm combined. Based on the results from this study, the authors highly recommend investigating discrepancies in data interpretation from different presentation types on the small micropores with sizes less than 2 nm that are measured by low-pressure CO$_2$ adsorption method since this pore size range are abundant in shales.

4. Conclusions

In order to understand how presenting pore size distribution data would affect the pore structure interpretation of shale rocks, three different main types of data presentations from $N_2$ adsorption and high-pressure mercury intrusion on several shale samples from the Bakken were compared. The main conclusions of this study can be listed as:

1. The $DV$ curve depends largely on the experimental data points spacing/intervals.

2. In $N_2$ adsorption, the deconvolution of the PSD curves showed that some peaks representing pore sizes around 10-40 nm exist in both $DV/Dd$ and $DV/D\log d$ curves. The $DV/Dd$ curve can provide us with more peaks in the smaller pore ranges compared to $DV/D\log d$. The heterogeneity index obtained from the $DV/Dd$ curve is more significant than the heterogeneity index from the $DV/D\log d$ curve. Linear correlations exist between the heterogeneity indexes from these two different presentations.

3. Considering high-pressure mercury intrusion, the location and the intensity of the peaks from the $DV/Dd$ and $DV/D\log d$ representing various pore radii found to differ. The heterogeneity index from the $DV/Dd$ curve was larger than the heterogeneity index from the $DV/D\log d$. The impact of rock compositions on the heterogeneity index of these two presentations was found to be similar.

4. $DV/Dd$ will incite the presence of smaller pore ranges and suppress the existence of larger pores while the $DV/D\log d$ has an opposite effect. When analysing the $N_2$ adsorption data, the $DV/Dd$ presentation should be picked based on the results from this study, while for analysing of the mercury intrusion data, the $DV/D\log d$ presentation is superior based on the pore sizes that each method can detect.

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**References**


Appendix

Deconvolution procedure (Ulm et al., 2007; Sorelli et al., 2008; Liu et al., 2017)
The pores in the samples can be divided into $J = 1, n$ pore size groups with sufficient contrast in pore size distributions. The $J_{th}$ pore group occupies a volume fraction $f_J$ of the total porosity. The theoretical probability density function (PDF) of the single phase, assuming to fit a normal distribution is defined as:

$$P_J(x_i, U_J, S_J) = \frac{2}{\sqrt{2\pi(S_J)^2}} \exp\left[\frac{-(x_i - U_J)^2}{2(S_J)^2}\right]$$  \hspace{1cm} (A.1)

where $U_J$ and $S_J$ are the mean value and the standard deviation of pore size distributions of the phase $J = 1$ to $n$.

After that, we minimize the difference between the data from the weighted model-phase PDF and the experimental PDF Eqs. (A.2) and (A.3):

$$\min \left\{ \sum_{i=1}^{m} \sum_{J=1}^{n} f_J P_J(x_i, U_J, S_J) - P_x(x_i) \right\}$$  \hspace{1cm} (A.2)

$$\sum_{J=1}^{n} f_J = 1$$  \hspace{1cm} (A.3)

In the above equation, $P_x(x_i)$ is the measured value of the normalized frequency of the pore size $x_i$ and $m$ is the number of the intervals (bins).

To ensure that the pore size groups have sufficient contrast, the overlap of successive Gaussian curves representative of the two phases is constrained by the following criterion:

$$U_J + S_J < U_{J+1} + S_{J+1}$$  \hspace{1cm} (A.4)